

THE KUWAITI MORTALITY RATES AND SOME COMPARISONS

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1. Introduction

Governments in many countries depend heavily upon estimate of future populations. Water storage facilities and electricity generating systems, for example, need long-term planning and as the demand for these utilities depends upon the size and structure of the populations, population surveys and projections are required well into the future. Projections are also needed to estimate future demand for kindergartens, schools, hospitals, playing fields, senior citizens facilities, old age pensions,.....etc.

In order to allow the Kuwaiti social security and pensions system in the future to fulfil its role, it is very important to study the characteristics of the Kuwaiti population, how they are attained and how they are changing [1].

In this paper , two abridged kuwaiti life tables are presented and analyzed. Also , a comparison between these rates have been done.

2. Availabilty of data

Kuwait has a good deal of demographic data collected through population censuses and vital registration system. Since 1957, seven regular censuses have been taken, the last one was conducted in April 1985. A system of vital registration which provides a fairly adequate amount of information on the dynamics of population was started only in 1964 through the introduction

of legislation for the compulsory [5]. Since then, serious efforts have had been made for the improvement of the registration system. In 1969, a new law was enacted for overcoming the shortcoming of the first legislation. Thus, from 1970 onwards, the vital registration system in Kuwait could be considered as more complete and reliable [4],[5].

3- Methodology

Various methods of constructing abridged life tables have been developed-among them, King's method (1914), Reed-Merrell's method (1939) and Greville's method (1943).

In this paper, the most recent method of Chiang (1961) is suggested to construct the Kuwaiti rates [3]. The idea and procedure used in the construction of the abridged life table by this method are the same as those used in the construction of the complete life table, except for differences that result from the length of intervals. The essential element here is the average fraction of interval lived by each person who dies at an age included in the interval. This fraction, denoted by a_i , is conceptually a logical extension of the fraction a_x , of the last year of life in the complete life table, which is often assigned a value of half on the assumption that deaths occur uniformly through out the year.

By definition [3], the fraction a_i of the interval lived by an individual who dies in the interval is.

$$a_i = \frac{\sum_{x=x_i}^{x_{i+1}} i p_x q_x ((x-x_i) + a'x)}{n_i (1 - i p_{i+i})} \quad (3.1)$$

we can rewrite equation(3.1) as follows:

$$a_i n_i = \frac{\sum_{x=x_i}^{x_{i+1}} i p_x q_x ((x-x_i) + a'x)}{1 - i p_{i+i}} \quad (3.2)$$

Here the coefficient

$$\frac{i p_x q_x}{1 - i p_{i+i}}, \quad x_i \leq x < x_{i+i} \quad (3.3)$$

is the proportion of those dying in the interval (x_i, x_{i+i}) , who will die in the year $(x, x+1)$, This shows that a_i depends neither on the values of q_x or p_x , nor on the specific death rate M_x , but rather on the trend of mortality within the interval.

When $a'_x = 1/2$ for $x_i \leq x < x_{i+i}$, equation (3.2) may be rewritten as.,

$$a_i n_i = \sum_{x=x_i}^{x_{i+1}} \frac{i p_x q_x}{1 - i p_{i+i}} \left[(x-x_i) + 1/2 \right] \quad (3.4)$$

Once we calculate the fractions using equation(3.4) it is easy to obtain q_i and M_i as follows .:

$$q_i = \frac{D_i}{N_i} \quad (3.5)$$

$$M_i = \frac{D_i}{(N_i - D_i)n_i + a_i n_i D_i} \quad (3.6)$$

where, N_i is the number of individuals alive at exact age x_i among whom D_i deaths occur in the interval, and M_i is the ratio of D_i to the total number of years lived by the N_i individuals during the interval (x_i, x_{i+i}) .

Solving equation (3.6) for N_i and substituting the resulting expression in (3.5), give the basic formula in the construction of an abridged life table,

$$q_i = \frac{n_i M_i}{1 + (1 - a_i) \frac{n_i M_i}{2}} \quad (3.7)$$

Further, using Freeman's simple formula [2], which assumes that $\frac{dP_x}{dx} \approx P_x^3 - P_{x+5}^2$, over the initial quinquennial age step and through out the table, we can extract the life functions, by sex, every fifth year of age separately for the Kuwaiti population.

All other quantities in the table are functions of q_i, a_i , and the radix l_0 . The number d_i of deaths in (x_i, x_{i+1}) and the number l_{i+1} of survivals at age x_{i+1} are computed from

$$d_i = l_i q_i \quad i = 0, 1, 2, \dots, w-1 \quad (3.8)$$

and

$$l_{i+1} = l_i - d_i \quad i = 0, 1, 2, \dots, w-1 \quad (3.9)$$

respectively. The number of years lived in the interval (x_i, x_{i+1}) by the l_i survivors at age x_i is

$$L_i = n_i (l_i - d_i) + a_i n_i d_i \quad i = 0, 1, 2, \dots, w-1 \quad (3.10)$$

The final age interval is again an open interval, and L is computed exactly as the complete life table.

$$L_w = l_w / M_w \quad (3.11)$$

where M_w is again the specific death rate for people of age x and over.

The total number T_i of years remaining to all the people obtaining age x_i is the sum of l_j for $j = i, i+1, \dots, w$. The observed expectation of life e_i age x_i is the ratio T_i / l_i , or

$$e_i = \frac{(L_i + L_{i+1} + \dots + L_w) / l_i}{l_i} \quad i = 0, 1, 2, \dots, w \quad (3.12)$$

4. Concluding Remarks :

The abridged life tables constructed on the basis of Chiang's method, referred above, are presented in four tables, see (Appendix I). According to these tables, the life expectancy at birth for 1965-1970 was 61.75 years for Kuwaiti males and 61.11 years for Kuwaiti females. During 1975-1980, the males life expectancy at birth has been improved to 66.39 years, and the females life expectancy has gained some improvement to become 71.99 years.

The Kuwaiti curves which are presented in appendix II, showing a decline during the early childhood years as the child adapts to the new environment and gains immunity from the diseases of the outside world, then the curves take the form of J-shape. In both periods, the probabilities of dying are high in infancy, fall to minimum in the age group (10,14), rise slowly toward middle life and thereafter rise rapidly with increasing age. The excess infant mortality appears to be related to several reasons [5]. First, it may be partly due to artifact of data. Second, the low education level of the Kuwaiti mothers is associated with higher infant mortality. Third, there is a widespread practice among Kuwaiti families to leave their children in the care of uneducated domestic servants who are often responsible for the preparation of feed for their infants at home. The presence of servants in the household is associated with higher infant mortality may be due to the uncontrolled fertility as births born with short interval are subject to comparatively high mortality. Fifth, the Kuwaiti

population consists of a large number Bedouin populations who have higher than average fertility and mortality rates and this may partly be responsible for sending the overall Kuwaiti infant mortality rates up.

Also, four tables are presented, see (Appendix III), which are showing that males and females mortality rates have been improved immensely at all ages except at some old ages. It is clear that female mortality is lower than male for almost all ages, the reasons of that, men tend to be exposed to more hazardous environmental factors, accidents and violence than women, and females also appear to be genetically superior.

R E F E R E N C E S :

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APPENDIX (I)

Table (I.1)
Abridged Life Table For Kuwaiti Females
1965-1970

| Age Group | q_i | l_i | n^d_i | a_i | n^L_i | T_i | e_i |
|--------------|----------|---------|---------|-------|---------|-----------|-------|
| 0- | .062550 | 100.000 | 6.255 | .14 | 95.622 | 6.711.321 | 67.11 |
| 1- | .021041 | 93.745 | 1.977 | .21 | 369.405 | 6.615.699 | 70.57 |
| 5- | .007672 | 91.768 | 704 | .23 | 456.906 | 6.246.294 | 68.07 |
| 10- | .005390 | 91.064 | 482 | .25 | 454.089 | 5.789.388 | 63.58 |
| 15- | .004183 | 90.582 | 379 | .33 | 451.970 | 5,335.299 | 58.91 |
| 20- | .006192 | 90.203 | 558 | .42 | 449.684 | 4,883.329 | 54.14 |
| 25- | .010311 | 89,645 | 924 | .42 | 446,520 | 4,433.645 | 49.46 |
| 30- | .010461 | 88.921 | 930 | .46 | 442.365 | 3,987.125 | 44.84 |
| 35- | .012843 | 87.991 | 1.130 | .47 | 437.268 | 3.544.760 | 40.29 |
| 40- | .015864 | 86.861 | 1.378 | .51 | 430.945 | 3,107.492 | 35.78 |
| 45- | .019000 | 85.483 | 1.624 | .51 | 423.453 | 2.676.547 | 31.31 |
| 50- | .031211 | 83.859 | 2.617 | .53 | 413.343 | 2.253.094 | 26.87 |
| 55- | .054373 | 81.242 | 4.417 | .57 | 395.955 | 1.839.751 | 22.65 |
| 60- | .084142 | 76.825 | 6.464 | .58 | 368.741 | 1.443.796 | 18.79 |
| 65- | .123242 | 70.361 | 8.671 | .61 | 331.113 | 1.075.055 | 15.27 |
| 70- | .187833 | 61.690 | 11.587 | .63 | 280.950 | 743.942 | 12.06 |
| 75- | .295070 | 50.103 | 14.748 | .55 | 214.577 | 462.992 | 9.24 |
| 80- | .424072 | 35.355 | 14.993 | .41 | 138.534 | 138.534 | 7.03 |
| 85- | .555103 | 20.362 | 11.303 | .32 | 71.549 | 109.881 | 5.40 |
| 90- | .571271 | 9.059 | 6.081 | .24 | 28.105 | 38.332 | 4.23 |
| 95- | 1.000000 | 2.978 | 2.978 | .11 | 10.227 | 10.227 | 3.43 |

Table (I.2)
Abridged Life Table For Kuwaiti Males
1965 - 1970

| Age Group | q_i | l_i | n^d_i | a_i | n^L_i | T_i | e_i |
|--------------|----------|---------|---------|-------|---------|-----------|-------|
| 0- | .071451 | 100.000 | 7.145 | .11 | 94.998 | 6.174.818 | 61.75 |
| 1- | .017650 | 92.855 | 1.639 | .17 | 367.159 | 6.079.820 | 65.48 |
| 5- | .009072 | 91.216 | 827 | .22 | 453.938 | 5.712.661 | 62.63 |
| 10- | .010061 | 90.389 | 909 | .31 | 449.733 | 5,258.723 | 58.18 |
| 15- | .011343 | 89.480 | 1.015 | .33 | 444.877 | 4.808.990 | 53.74 |
| 20 | .012040 | 88.465 | 1.065 | .37 | 439.731 | 4.364.113 | 49.33 |
| 25- | 0.14114 | 87.400 | 1.233 | .37 | 433.981 | 3,924.382 | 44.90 |
| 30- | .016151 | 86.167 | 1.392 | .42 | 427.405 | 3,490.401 | 40.51 |
| 35- | .018112 | 84.775 | 1.535 | .42 | 420.154 | 3.062.996 | 36.13 |
| 40- | .022243 | 83.240 | 1.851 | .48 | 411.756 | 2.642.842 | 31.75 |
| 45- | .032260 | 81.389 | 2.626 | .48 | 400.829 | 2.231.086 | 27.41 |
| 50- | .050281 | 78.763 | 3.960 | .53 | 384.325 | 1.830.257 | 23.24 |
| 55- | .082510 | 74.703 | 6.164 | .53 | 359.064 | 1.445.932 | 19.36 |
| 60- | .129611 | 68.539 | 8.883 | .56 | 321.649 | 1.086.868 | 15.86 |
| 65- | .198154 | 59.656 | 11.821 | .61 | 269.728 | 765.219 | 12.83 |
| 70- | .275533 | 47.835 | 13.180 | .63 | 206.331 | 495.491 | 10.35 |
| 75- | .356022 | 34.655 | 12.338 | .52 | 141.677 | 289.160 | 8.34 |
| 80- | .453110 | 33.317 | 10.112 | .41 | 83.354 | 147.483 | 6.61 |
| 85- | .583041 | 12.205 | 7.116 | .35 | 41.797 | 62.129 | 5.09 |
| 90- | .695623 | 5.089 | 3.540 | .27 | 15.333 | 20.332 | 3.99 |
| 95- | 1.000000 | 1.549 | 1.549 | .11 | 4.999 | 4.9999 | 3.23 |

Table (I.3)
Abridged Life Table For Kuwaiti Females
1975 - 1980

| Age Group | $n q_i$ | l_i | $n d_i$ | a_i | $n L_i$ | T_i | e_i |
|--------------|----------|---------|---------|-------|---------|-----------|-------|
| 0- | .036700 | 100.000 | 3.670 | .12 | 95.917 | 7.198.818 | 71.99 |
| 1- | .008896 | 96.330 | 857 | .34 | 386.912 | 7,061.336 | 73.30 |
| 5- | .002799 | 95.473 | 267 | .36 | 476.697 | 6.674.424 | 69.91 |
| 10- | .001606 | 95.206 | 153 | .38 | 475.647 | 6.197.727 | 65.10 |
| 15- | .002136 | 95.053 | 203 | .42 | 474.757 | 5.722.080 | 60.20 |
| 20- | .003113 | 94.850 | 295 | .46 | 473.512 | 5.247.323 | 55.32 |
| 25- | .004478 | 94.555 | 423 | .46 | 471.717 | 4.773.811 | 50.49 |
| 30- | .005982 | 94.132 | 563 | .48 | 469.252 | 4.302.094 | 45.70 |
| 35- | .008186 | 93.569 | 766 | .51 | 465.930 | 3.832.842 | 40.96 |
| 40- | .011535 | 92.803 | 1.070 | .52 | 461.340 | 3.366.912 | 36.28 |
| 45- | .020394 | 91.733 | 1.871 | .54 | 453.987 | 2.905.572 | 31.67 |
| 50- | .029084 | 89.862 | 2.613 | .58 | 442.777 | 2.451.585 | 27.28 |
| 55- | .050168 | 87.249 | 4.377 | .62 | 425.302 | 2.008.808 | 23.02 |
| 60- | .073558 | 82.872 | 6.096 | .63 | 399.120 | 1.583.506 | 19.11 |
| 65- | .128246 | 76.776 | 9.846 | .58 | 359.265 | 1.184.386 | 15.43 |
| 70- | .189987 | 66.930 | 12.716 | .51 | 302.860 | 825.121 | 12.33 |
| 75- | .294502 | 54.214 | 15.966 | .48 | 231.155 | 522.261 | 9.63 |
| 80- | .465858 | 38.248 | 15.525 | .48 | 152.433 | 291.106 | 7.61 |
| 85- | .532550 | 22.725 | 12.102 | .48 | 83.370 | 138.673 | 6.10 |
| 90- | .561371 | 10.623 | 5.963 | .32 | 38.208 | 55.303 | 5.21 |
| 95- | 1.000000 | 4.660 | 4.660 | .13 | 17.095 | 17.095 | 3.67 |

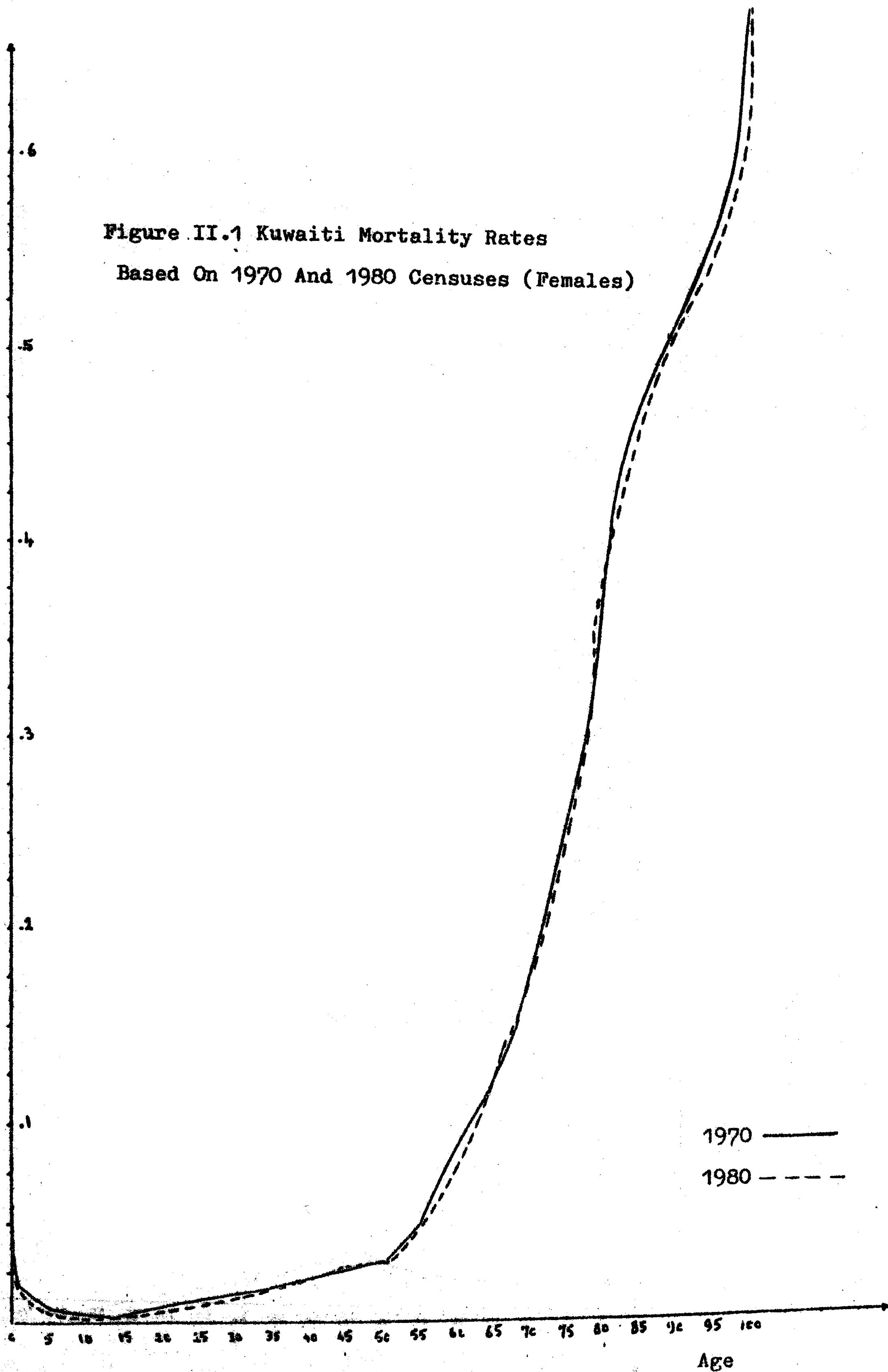
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Abridged Life Table For Kuwaiti Males
1975 - 1980

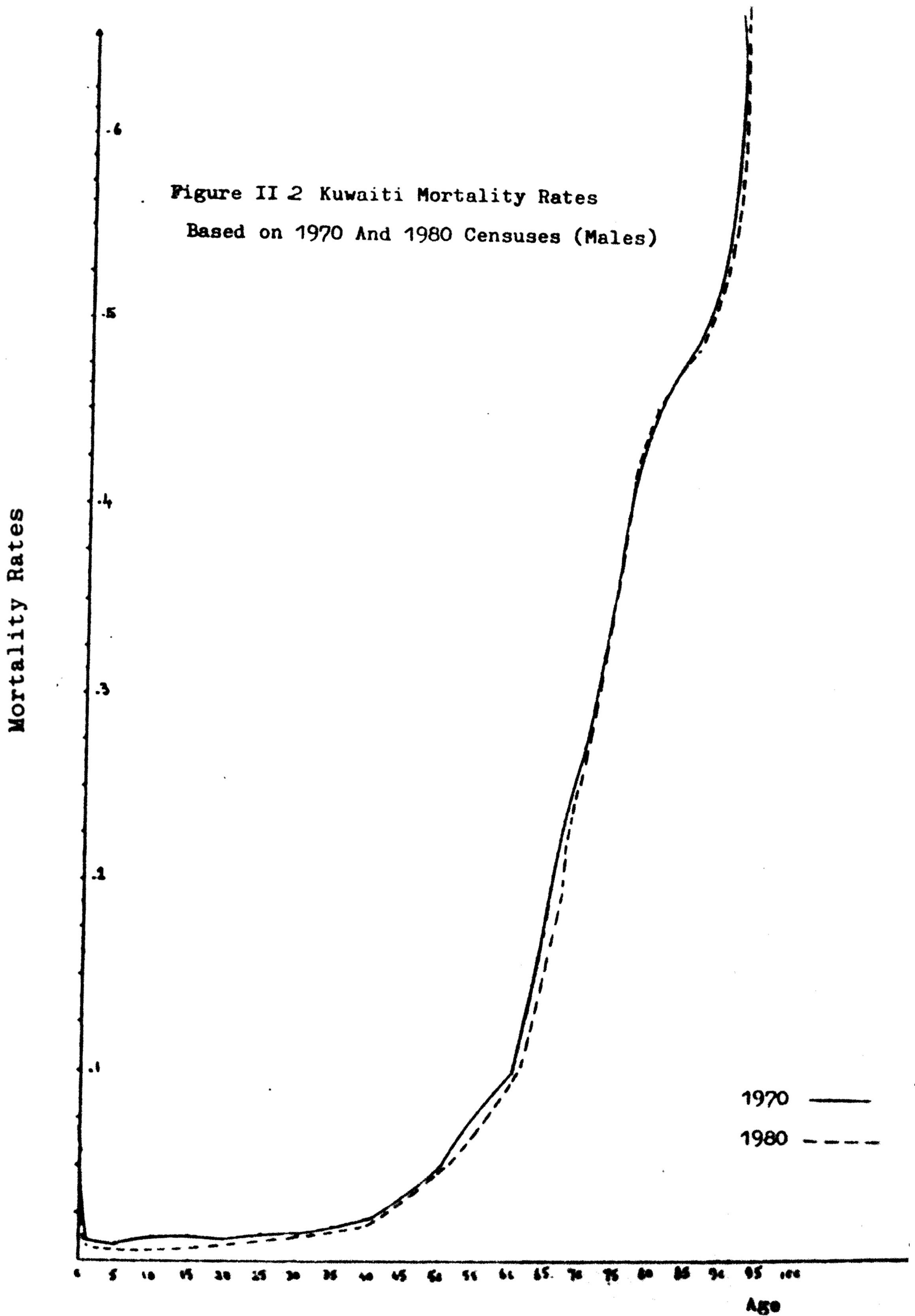
| Age Group | nq_i | l_i | n^d_i | a_i | n^L_i | T_i | e_i |
|--------------|----------|---------|---------|-------|----------|-----------|-------|
| 0- | .040500 | 100.000 | 4.050 | .14 | 96.593 | 6.638.986 | 66.39 |
| 1- | .009531 | 95.950 | 914 | .23 | 3385.740 | 6.542.393 | 68.19 |
| 5- | .004590 | 95.036 | 436 | .32 | 474.090 | 6.156.653 | 64.78 |
| 10- | .004201 | 94.600 | 397 | .42 | 472.007 | 5.692.563 | 60.06 |
| 15- | .005752 | 94.203 | 542 | .42 | 469.660 | 5.210.556 | 55.31 |
| 20- | .007490 | 93.661 | 702 | .48 | 466.550 | 4.740.896 | 50.61 |
| 25- | .009279 | 92.959 | 863 | .48 | 462.637 | 4.274.346 | 45.98 |
| 30- | .011592 | 92.096 | 1.068 | .51 | 457.810 | 3.811.709 | 41.39 |
| 35- | .014495 | 91.028 | 1.319 | .53 | 451.842 | 3.333.899 | 36.84 |
| 40- | .019859 | 89.709 | 1.781 | .53 | 444.092 | 2.902.057 | 32.35 |
| 45- | .031244 | 87.928 | 2.747 | .58 | 432.773 | 2.457.965 | 27.95 |
| 50- | .049074 | 85.181 | 4.180 | .61 | 415.455 | 2.025.192 | 23.78 |
| 55- | .079523 | 81.001 | 6.441 | .63 | 388,902 | 1.609.737 | 19.87 |
| 60- | .116875 | 74.560 | 8.714 | .52 | 351.015 | 1.220.835 | 16.37 |
| 65- | .184961 | 65.846 | 12.179 | .43 | 298.782 | 869.820 | 13.21 |
| 70- | .258762 | 53.667 | 13.887 | .36 | 233.617 | 571.038 | 10.64 |
| 75- | .362332 | 39.780 | 14.414 | .32 | 162.865 | 337.421 | 8.48 |
| 80- | .488247 | 25.366 | 12.385 | .32 | 95.867 | 174.556 | 6.88 |
| 85- | .535200 | 12.981 | 6.947 | .31 | 47.538 | 78.689 | 6.06 |
| 90- | .551240 | 6.034 | 3.326 | .24 | 21.855 | 31.151 | 5.16 |
| 95- | 1.000000 | 2.708 | 2.708 | .14 | 9.296 | 9.296 | 3.43 |

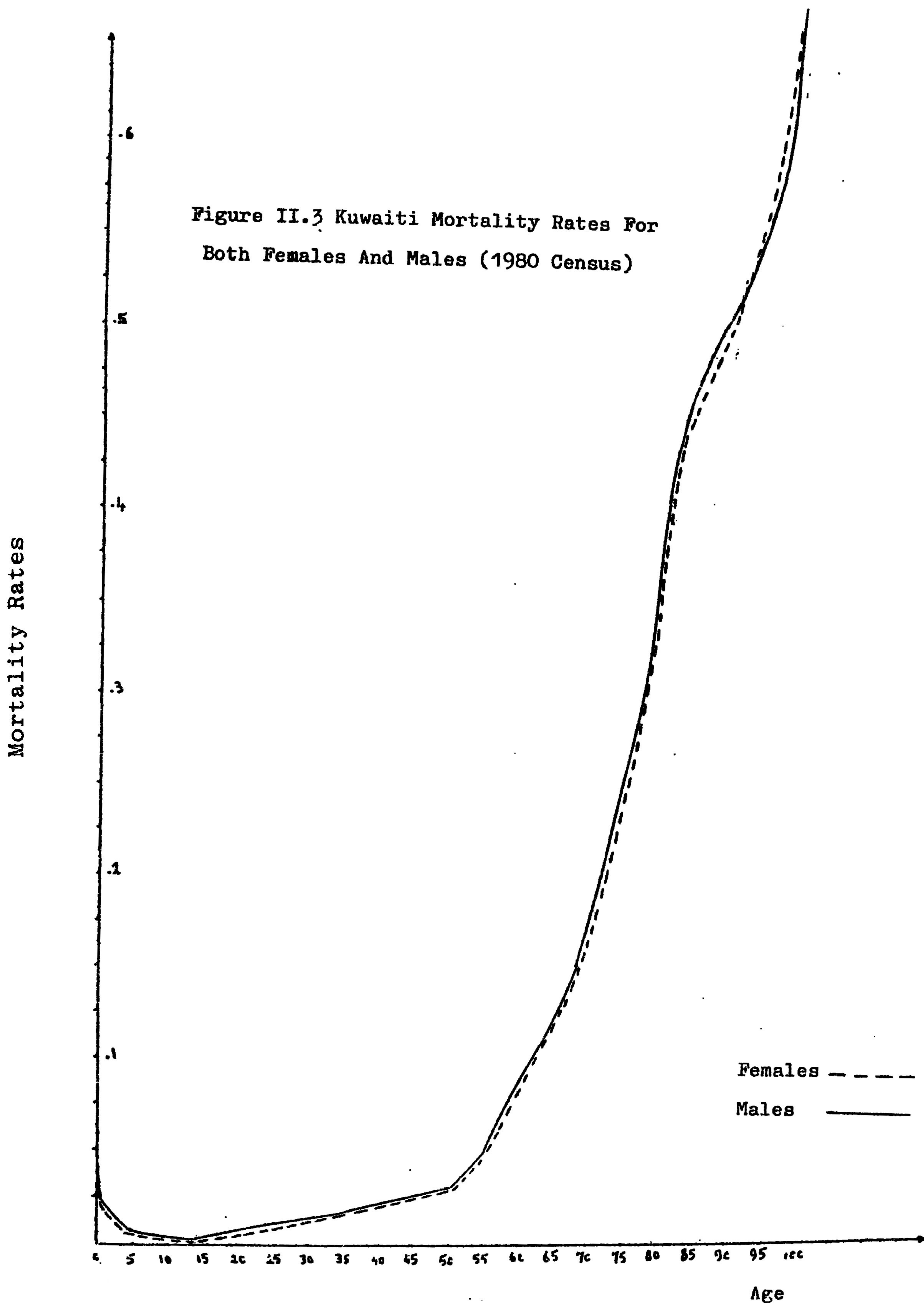
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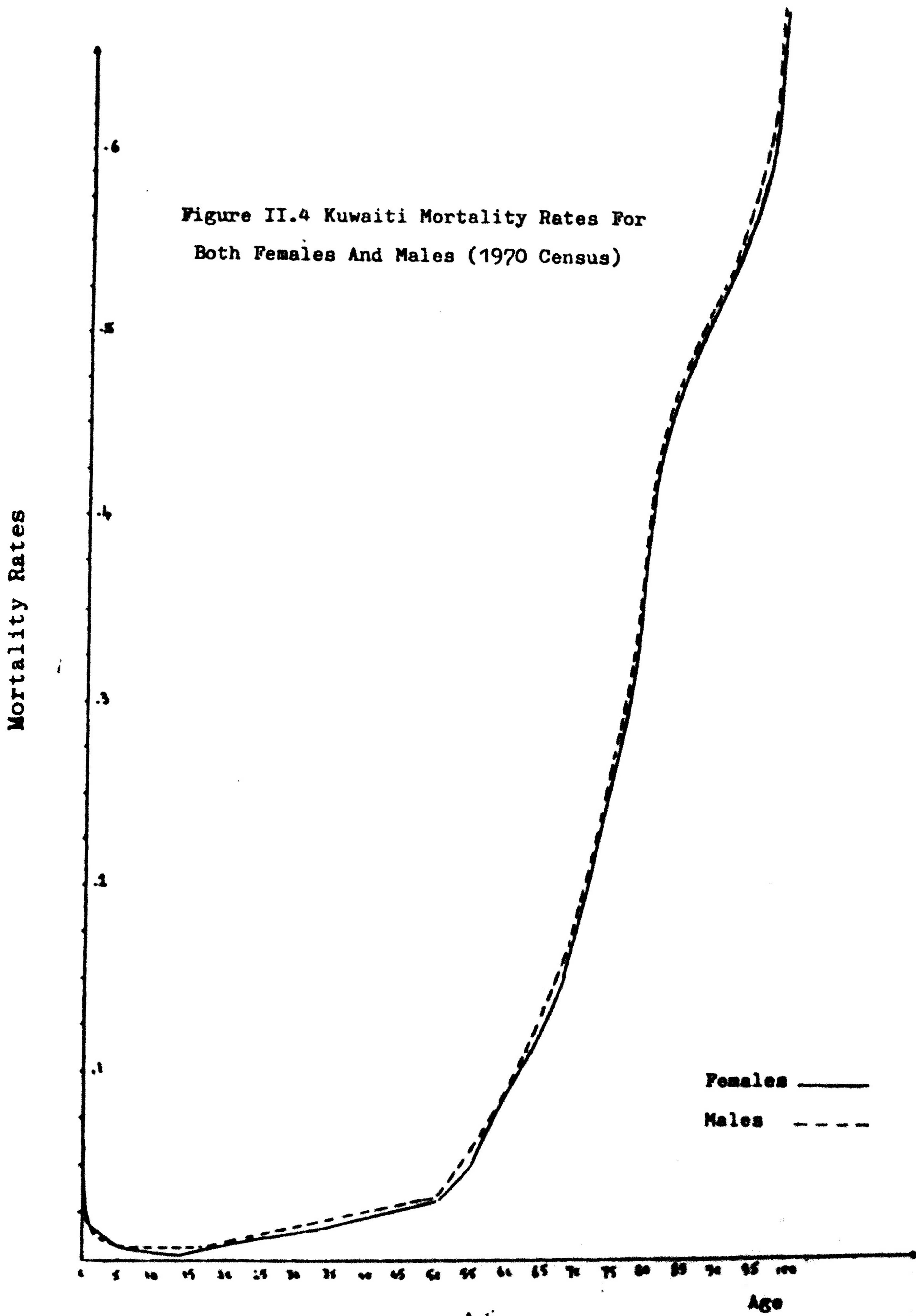
Mortality Rates

Figure II.1 Kuwaiti Mortality Rates
Based On 1970 And 1980 Censuses (Females)









A P P E N D I X (I I I)

Table (III.1)
Comparison Between Mortality Rates (Females)
1970 - 1980

| Age Group | n^S_i | | Ratio (2/1) |
|--------------|-------------|-------------|-------------|
| | 1970 (1) | 1980 (2) | |
| 0- | 0.062550 | 0.036700 | 58.67 |
| 1- | 0.021041 | 0.008896 | 42.28 |
| 15- | 0.007672 | 0.002799 | 36.49 |
| 10- | 0.005390 | 0.001606 | 29.80 |
| 15- | 0.004183 | 0.002136 | 51.10 |
| 20- | 0.006192 | 0.003113 | 50.29 |
| 25- | 0.010311 | 0.004478 | 43.43 |
| 30- | 0.010461 | 0.005982 | 57.19 |
| 35- | 0.012843 | 0.008186 | 63.75 |
| 40- | 0.015864 | 0.011535 | 72.73 |
| 45- | 0.019000 | 0.020394 | 107.33 |
| 50- | 0.031211 | 0.029084 | 93.19 |
| 55- | 0.054373 | 0.050168 | 92.27 |
| 60- | 0.084142 | 0.073558 | 87.42 |
| 65- | 0.123242 | 0.128246 | 104.06 |
| 70- | 0.187833 | 0.189907 | 101.15 |
| 75- | 0.295070 | 0.294502 | 99.81 |
| 80- | 0.424072 | 0.465858 | 109.85 |
| 85- | 0.555103 | 0.532550 | 95.94 |
| 90- | 0.571271 | 0.561371 | 98.27 |
| 95+ | 1.000000 | 1.000000 | 100.00 |

Table (III.2)
Comparison Between Mortality Rates (Males)
1970 - 1980

| Age Group | nq_i | | Ratio (2/1) % |
|--------------|-------------|-------------|------------------|
| | 1970 (1) | 1980 (2) | |
| 0- | 0.071451 | 0.040500 | 56.68 |
| 1- | 0.017650 | 0.009531 | 54.00 |
| 5- | 0.009072 | 0.004590 | 50.61 |
| 10- | 0.010061 | 0.004201 | 41.76 |
| 15- | 0.011343 | 0.005752 | 50.71 |
| 20- | 0.012040 | 0.007490 | 62.21 |
| 25- | 0.014114 | 0.011592 | 71.74 |
| 30- | 0.016151 | 0.011592 | 71.78 |
| 35- | 0.018112 | 0.014495 | 80.04 |
| 40- | 0.022243 | 0.019859 | 89.28 |
| 45- | 0.032260 | 0.031244 | 96.85 |
| 50- | 0.050281 | 0.049074 | 97.60 |
| 55- | 0.082510 | 0.079523 | 96.38 |
| 60- | 0.129611 | 0.116875 | 90.17 |
| 65- | 0.198154 | 0.184961 | 93.34 |
| 70- | 0.275533 | 0.258762 | 93.91 |
| 75- | 0.356022 | 0.362332 | 101.77 |
| 80- | 0.453110 | 0.488247 | 107.75 |
| 85- | 0.583041 | 0.535200 | 91.79 |
| 90- | 0.695623 | 0.551240 | 79.24 |
| 95+ | 1.000000 | 1.000000 | 100.00 |

Table (III.3)
Comparison Between Females and Males Mortality Rates
1970

| Age Group | $n q_i$ | | Ratio (1.2) % |
|--------------|-----------------|-----------------|------------------|
| | 1970 (F) (1) | 1970 (M) (2) | |
| 0- | 0.062550 | 0.071451 | 87.54 |
| 1- | 0.021041 | 0.017650 | 119.21 |
| 5- | 0.007672 | 0.009072 | 84.57 |
| 10- | 0.005390 | 0.010061 | 53.57 |
| 15- | 0.004183 | 0.011343 | 36.88 |
| 20- | 0.006192 | 0.012040 | 51.43 |
| 25 | 0.010311 | 0.014114 | 73.06 |
| 30 | 0.010461 | 0.116151 | 64.77 |
| 35- | 0.012843 | 0.018112 | 70.90 |
| 40- | 0.015864 | 0.022243 | 71.32 |
| 50- | 0.031211 | 0.050281 | 62.07 |
| 55- | 0.054373 | 0.082510 | 65.90 |
| 60- | 0.084142 | 0.129611 | 64.92 |
| 65- | 0.123242 | 0.198154 | 62.20 |
| 70- | 0.187833 | 0.275533 | 68.17 |
| 75- | 0.245070 | 0.356022 | 68.84 |
| 80- | 0.424072 | 0.453110 | 93.59 |
| 85- | 0.555103 | 0.583041 | 95.21 |
| 90- | 0.571271 | 0.695623 | 82.12 |
| 95+ | 1.000000 | 1.000000 | 100.00 |

Table (III.4)
Comparison Between Females and Males Mortality Rates
1980

| Age Group | $n q_i$ | | Ratio (1/2) % |
|--------------|-----------------|-----------------|------------------|
| | 1980 (F) (1) | 1980 (M) (2) | |
| 0- | 0.036700 | 0.040500 | 90.62 |
| 1- | 0.008896 | 0.009531 | 93.34 |
| 5- | 0.002799 | 0.004590 | 60.94 |
| 10- | 0.001606 | 0.004201 | 38.23 |
| 15- | 0.002136 | 0.005752 | 37.13 |
| 20- | 0.003113 | 0.007490 | 41.56 |
| 25- | 0.004478 | 0.009279 | 48.26 |
| 30- | 0.005982 | 0.011592 | 51.60 |
| 35- | 0.008186 | 0.014495 | 56.47 |
| 40- | 0.011535 | 0.019859 | 58.08 |
| 45- | 0.020394 | 0.031244 | 65.27 |
| 50- | 0.029084 | 0.049074 | 59.27 |
| 55- | 0.050168 | 0.079523 | 63.09 |
| 60- | 0.073558 | 0.116875 | 62.94 |
| 65- | 0.128246 | 0.184961 | 69.34 |
| 70- | 0.189987 | 0.258762 | 73.42 |
| 75- | 0.294502 | 0.362332 | 81.28 |
| 80- | 0.465858 | 0.488247 | 95.41 |
| 85- | 0.532550 | 0.535200 | 99.00 |
| 90- | 0.561370 | 0.551240 | 101.00 |
| 95+ | 1.000000 | 1.000000 | 100.00 |